

**High-resolution simulations  
of the final assembly of  
Earth-like planets I.  
Terrestrial accretion and  
dynamics**

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# What to Expect

- Background- formation of terrestrial planets
- Need for High Resolution
- Numerical Method
- Initial conditions
- Simulation 0
- Simulations 1a and 1b
- Simulations 2a and 2b
- Conclusions

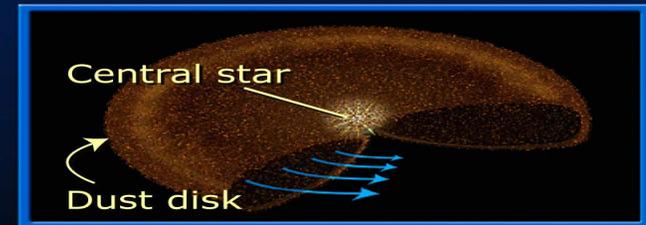


# Final Stages of Formation for Terrestrial planets

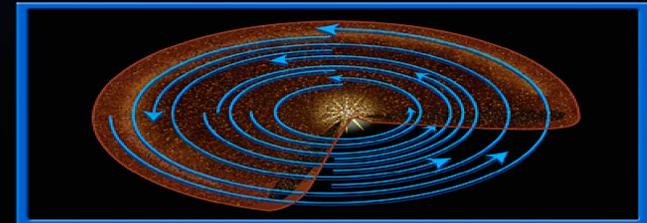
- Formation of planetary embryos from planetesimals
- Accretion of embryos into terrestrial planets
- Embryos form in two steps : Runaway and oligarchic growth

## TWO PLANET FORMATION

### Accretion model



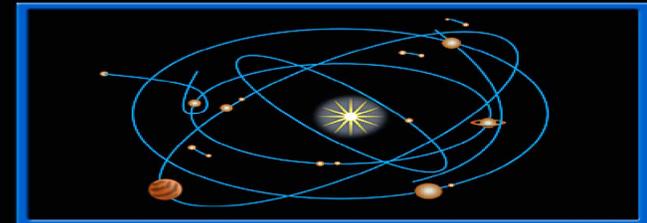
Orbiting dust grains accrete into "planetesimals" through nongravitational forces.



Planetesimals grow, moving in near-coplanar orbits, to form "planetary embryos."



Gas-giant planets accrete gas envelopes before disk gas disappears.



Gas-giant planets scatter or accrete remaining planetesimals and embryos.

# More about Embryos

- 30-50 or 500-1000 embryos formed, depending on mass
- Embryos form faster closer to the Sun
- Formation time unknown:  $10^4 - 10^7$  years
- Oligarchic growth ends when 50%-50% mass in embryos and planetesimals
- Final assembly - accretional growth – 50Myr



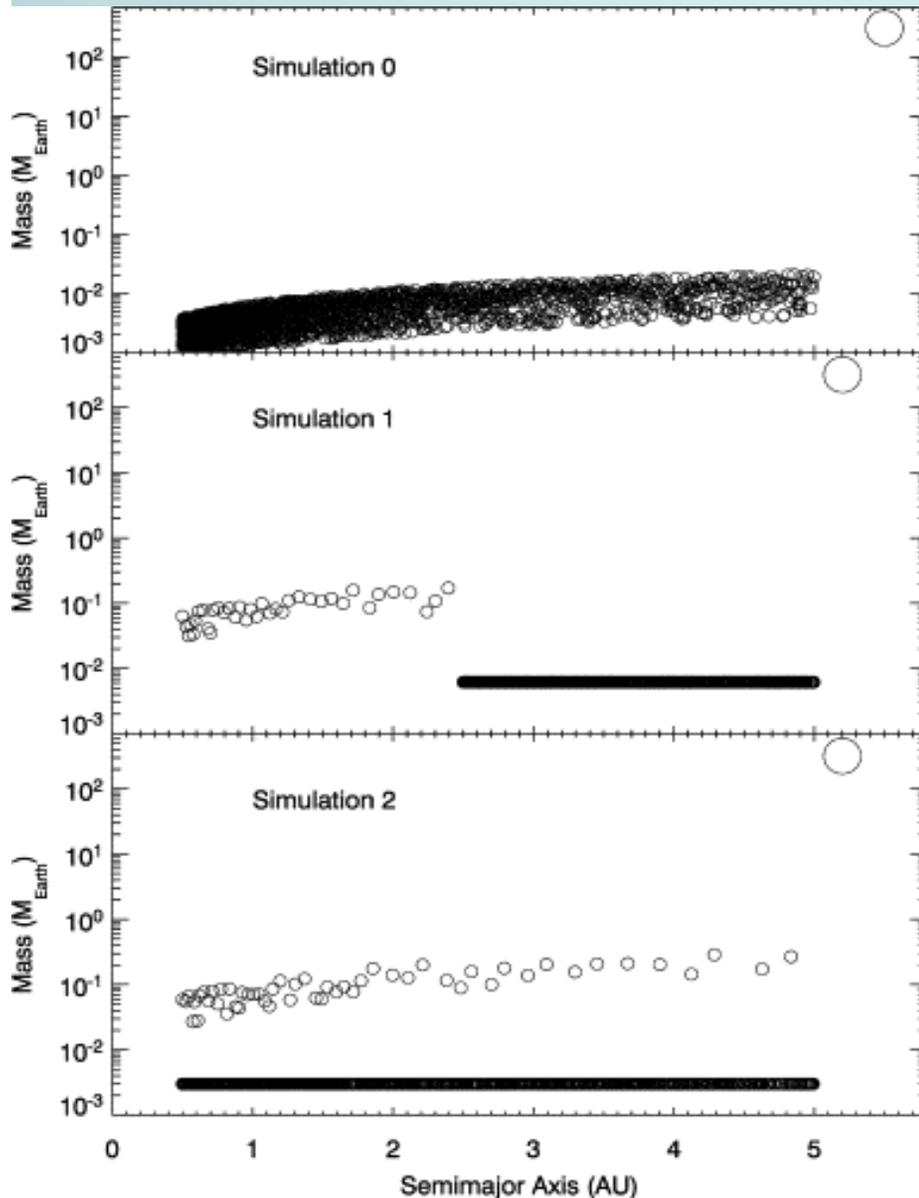
# Why High-Resolution Simulations?

- Past simulations limited to 20-200 particles, no sub-lunar size embryos, neglected planetesimals
- Dynamical friction requires large number of particles
- Large number low-resolution
- need better resolution to understand phenomena
- Simulate realistic number of embryos
- Problem- only one simulation and stochastic nature of accretion process

# Numerical Method

- Mercury- serial code (Chambers, 1999)
- 5-10X more particles compared to pervious simulations
- Time for simulation scales with number of particles  $N^2$
- 2-16 months of CPU time per simulation run

# INITIAL CONDITIONS



Initial conditions for 5 high resolution simulations

Simulation	$N$ (massive) <sup>a</sup>	$N$ (non-int) <sup>b</sup>	$M_{\text{TOT}}$ ( $M_{\oplus}$ ) <sup>c</sup>	$a_{\text{Jup}}$ (AU) <sup>d</sup>
0	1885	–	9.9	5.5
1a	1038	–	9.3	5.2
1b	38	1000	9.3	5.2
2a	1054	–	8.6	5.2
2b	54	1000	8.6	5.2

<sup>a</sup> Number of massive, self-interacting particles.

<sup>b</sup> Number of non-self-interacting particles.

<sup>c</sup> Total solid mass in planetary embryos and planetesimals.

<sup>d</sup> Orbital radius of Jupiter-mass giant planet.

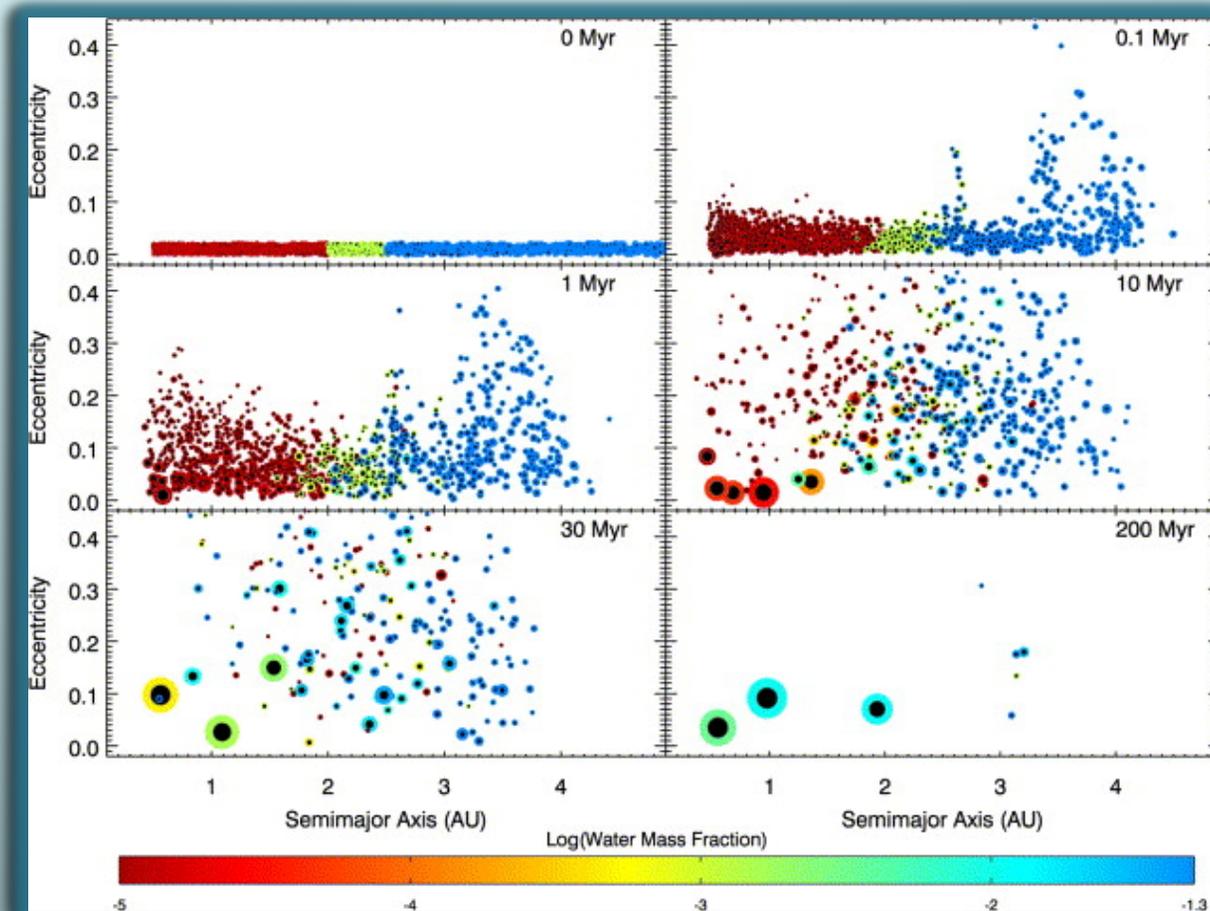
# Initial Conditions

- Represent different timescales for the formation of Jupiter and/or formation of embryos
- Did embryos form in the asteroid belt before Jupiter?
- Fast scenario- formed in inner disk before Jupiter
- Slow scenario-embryos start to accrete after Jupiter is formed
- 0-fast formation of Jupiter
- 1- late formation of Jupiter or slow accretion of embryos
- 2 - very late formation of Jupiter or fast embryo formation

# Simulation 0

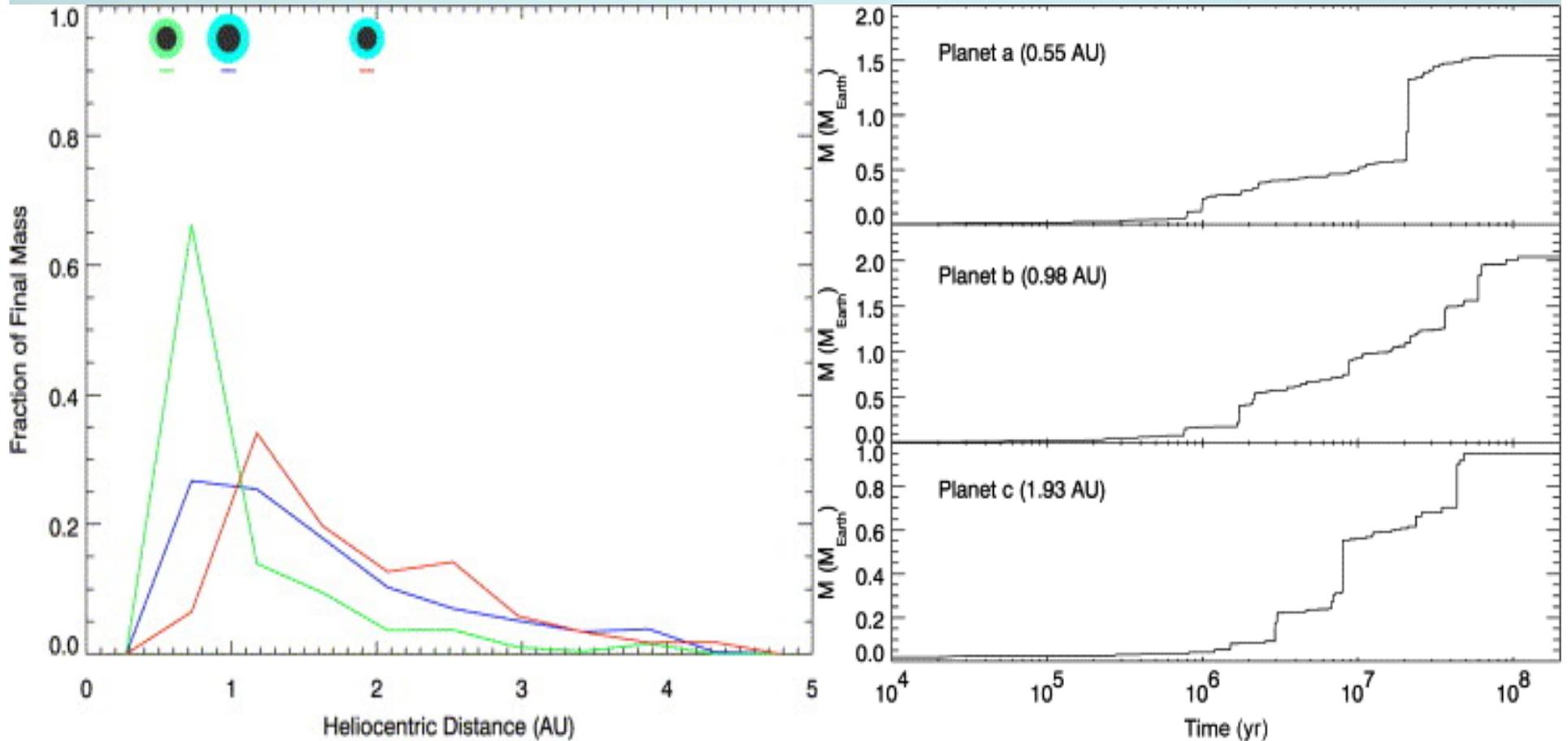
- Starts- Late stage of oligarchic growth
- No planetary embryos formed
- Embryo separation – 0.3 and 0.6 mutual Hill radii
- 1885 Planetesimals
- Simulation runs for 200 Myrs

# 1885 Particles and self-interacting

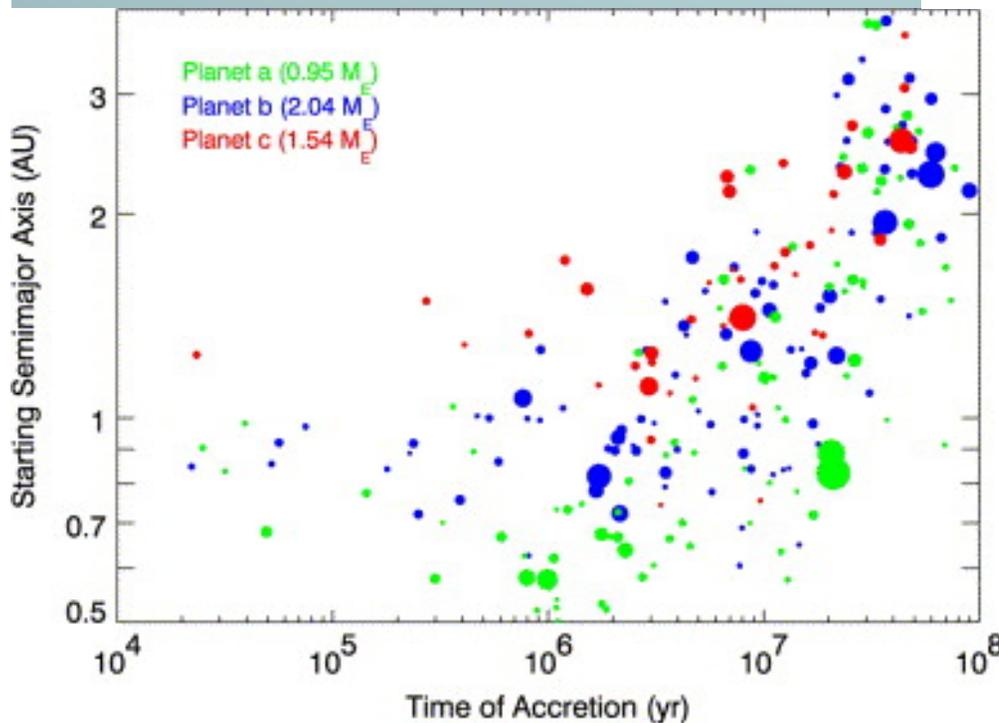
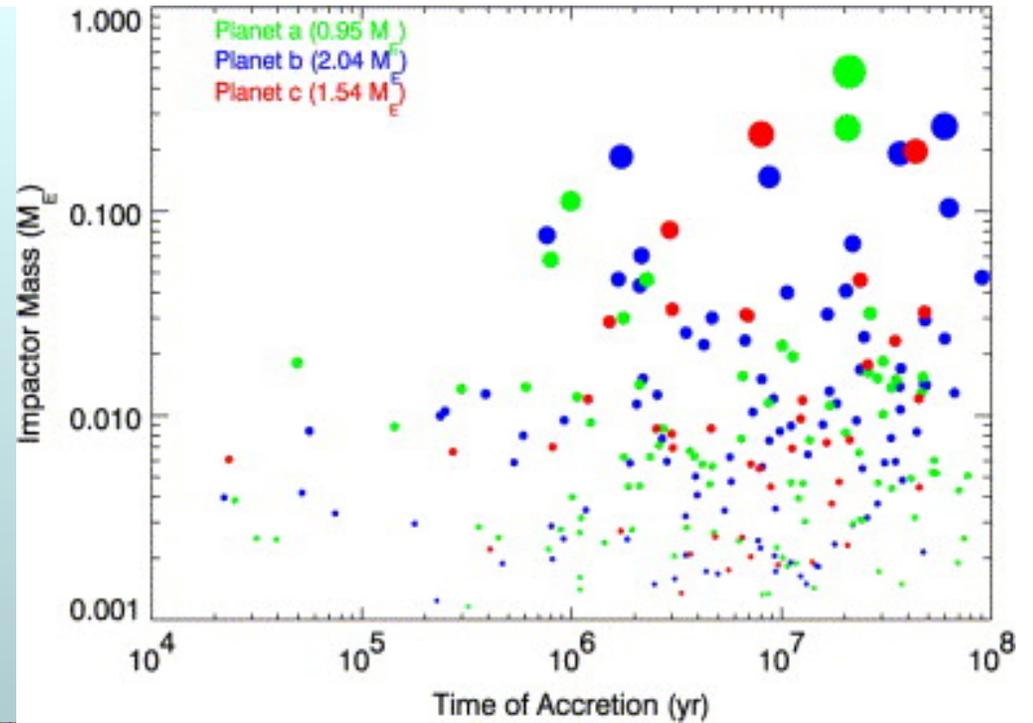


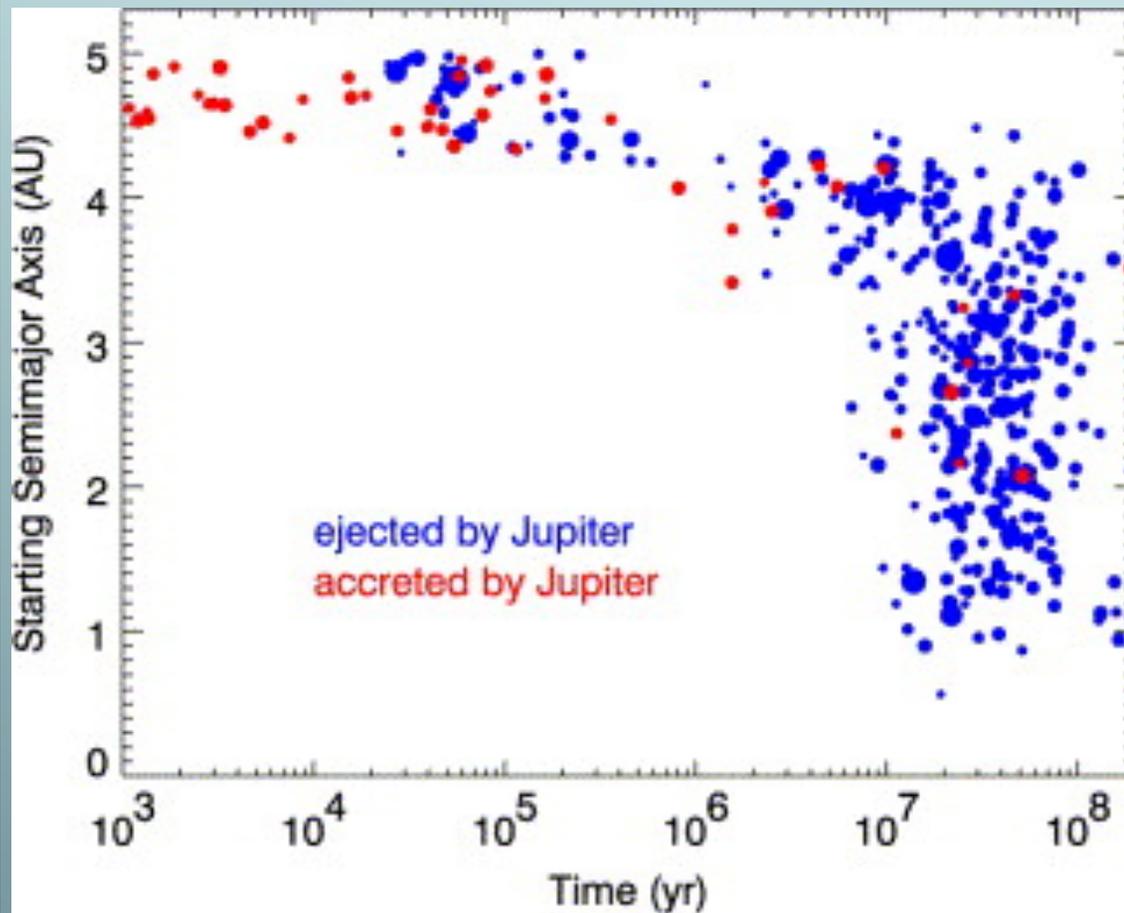
The size of each body corresponds to its relative physical size (i.e., its mass  $M^{1/3}$ ), but is not to scale on the x axis. The color of each particle represents its water content, and the dark inner circle represents the relative size of its iron core.

# The Feeding Zones!



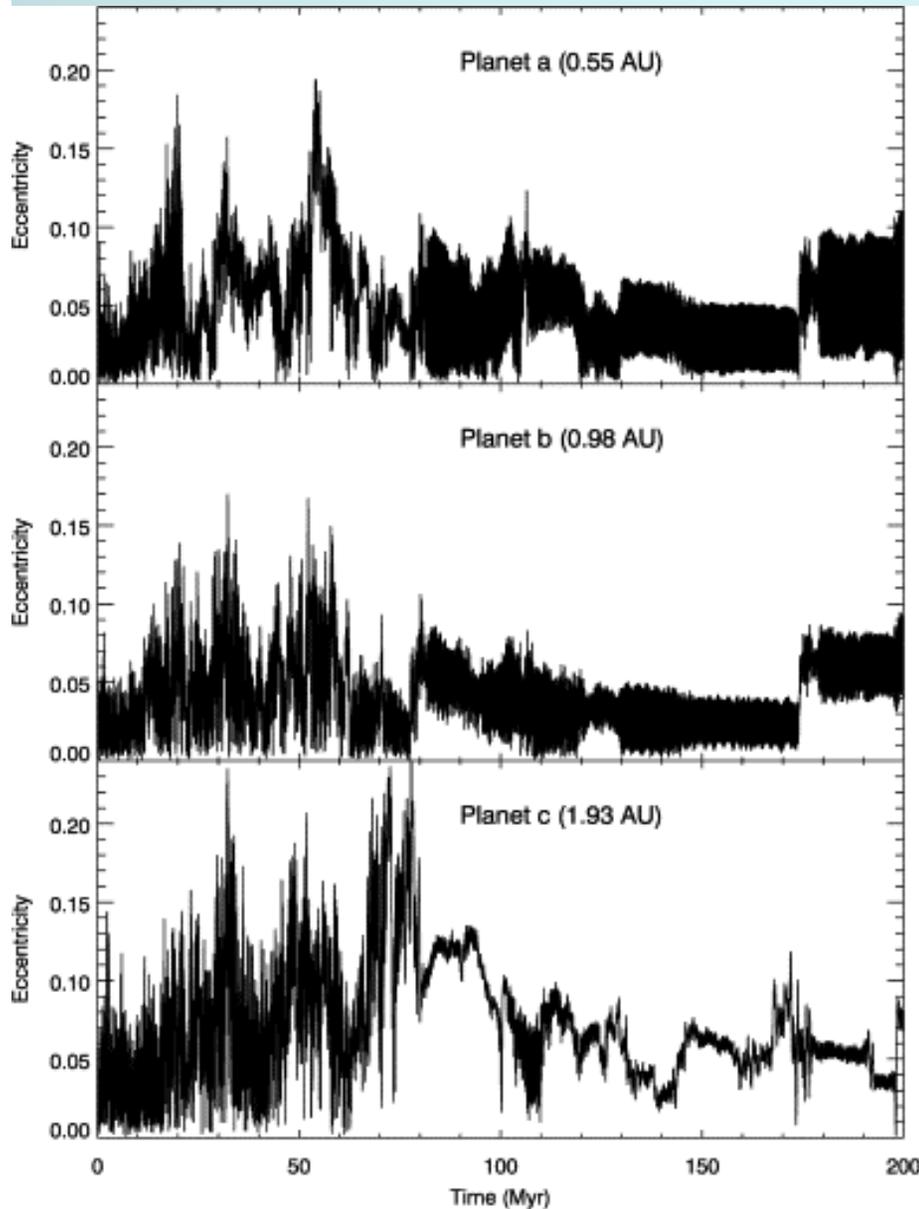
Accretion of more distant bodies marks the end of oligarchic growth in a region



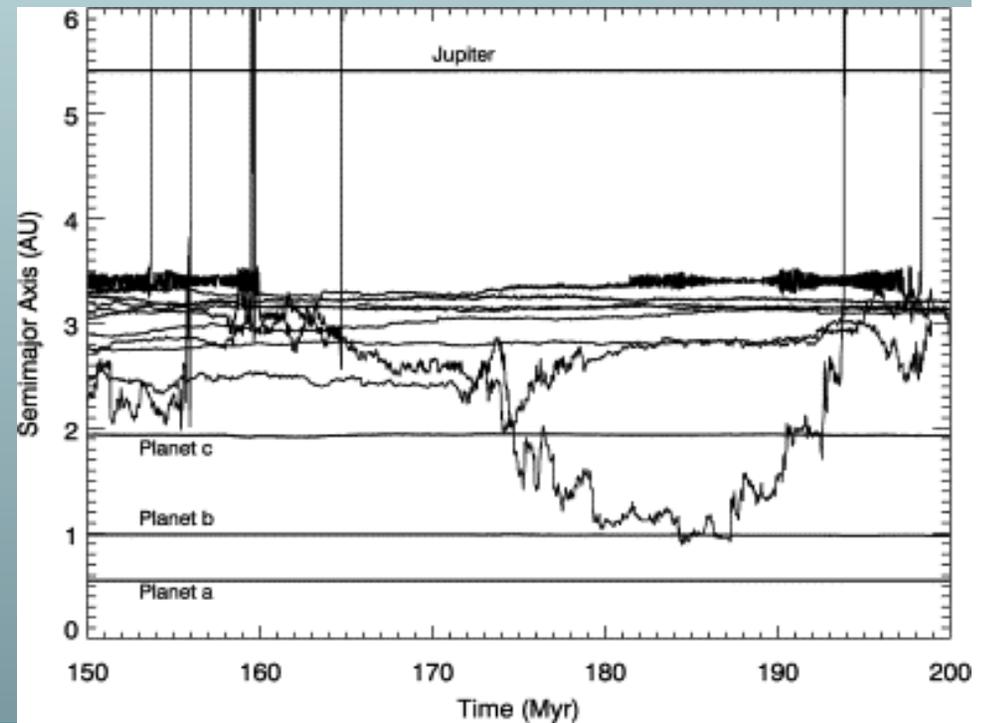


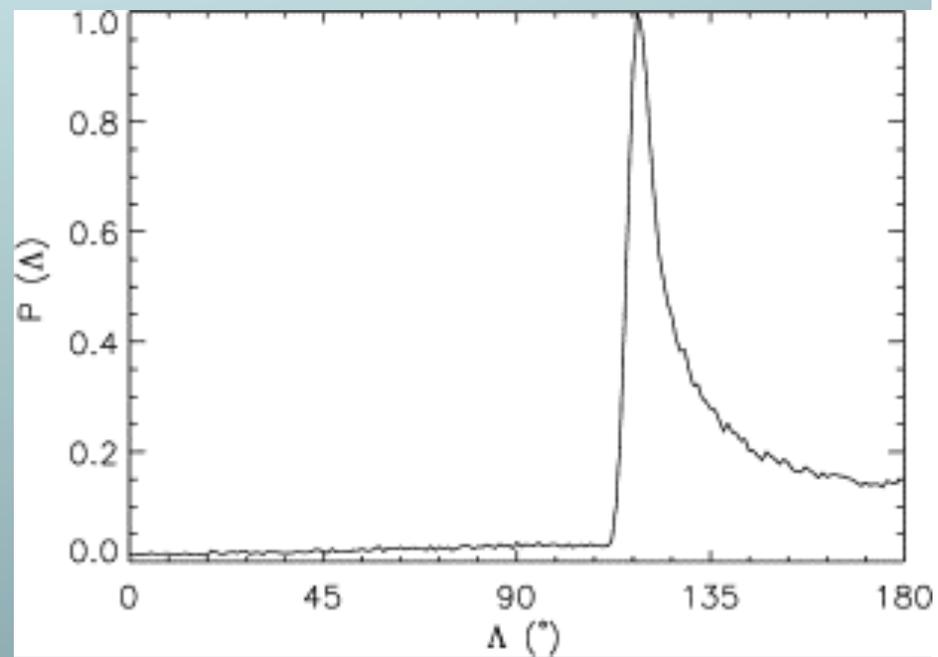
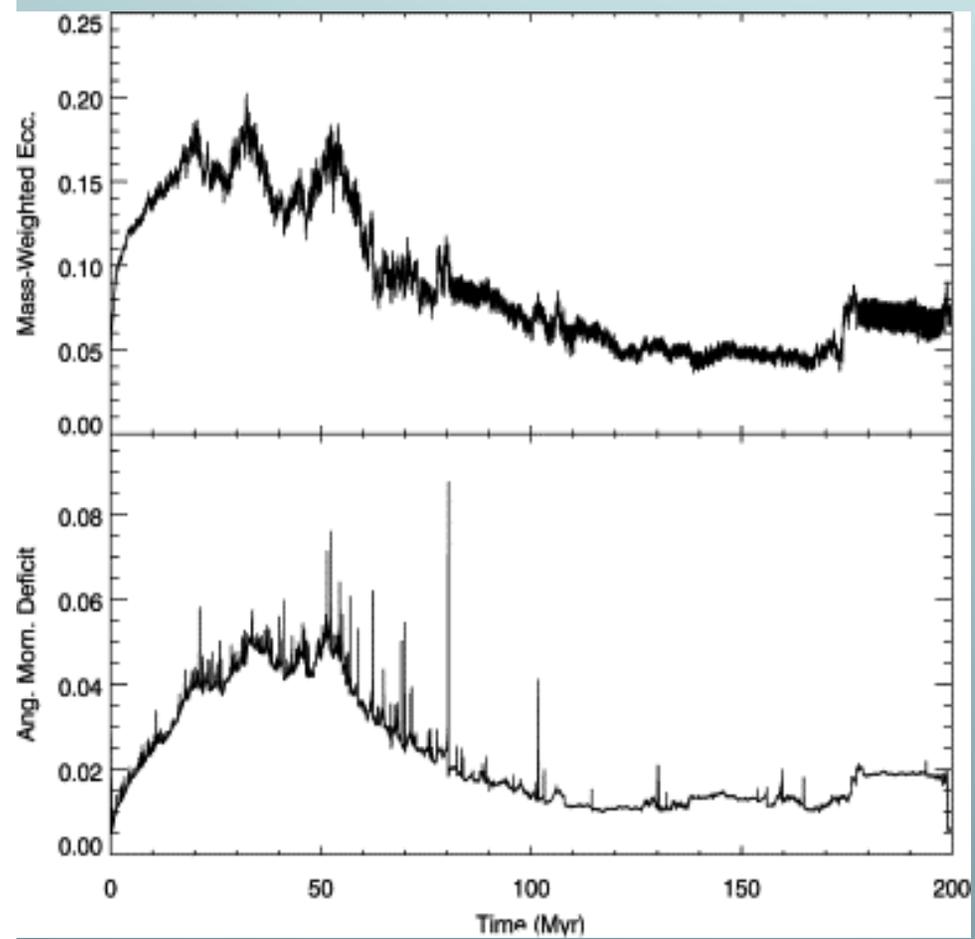
The timing of the ejection and accretion by Jupiter of bodies from different starting locations. Note the change in the “ejection zone” at  $t \approx 10 \text{ Myr}$ .

# Eccentricity vs time

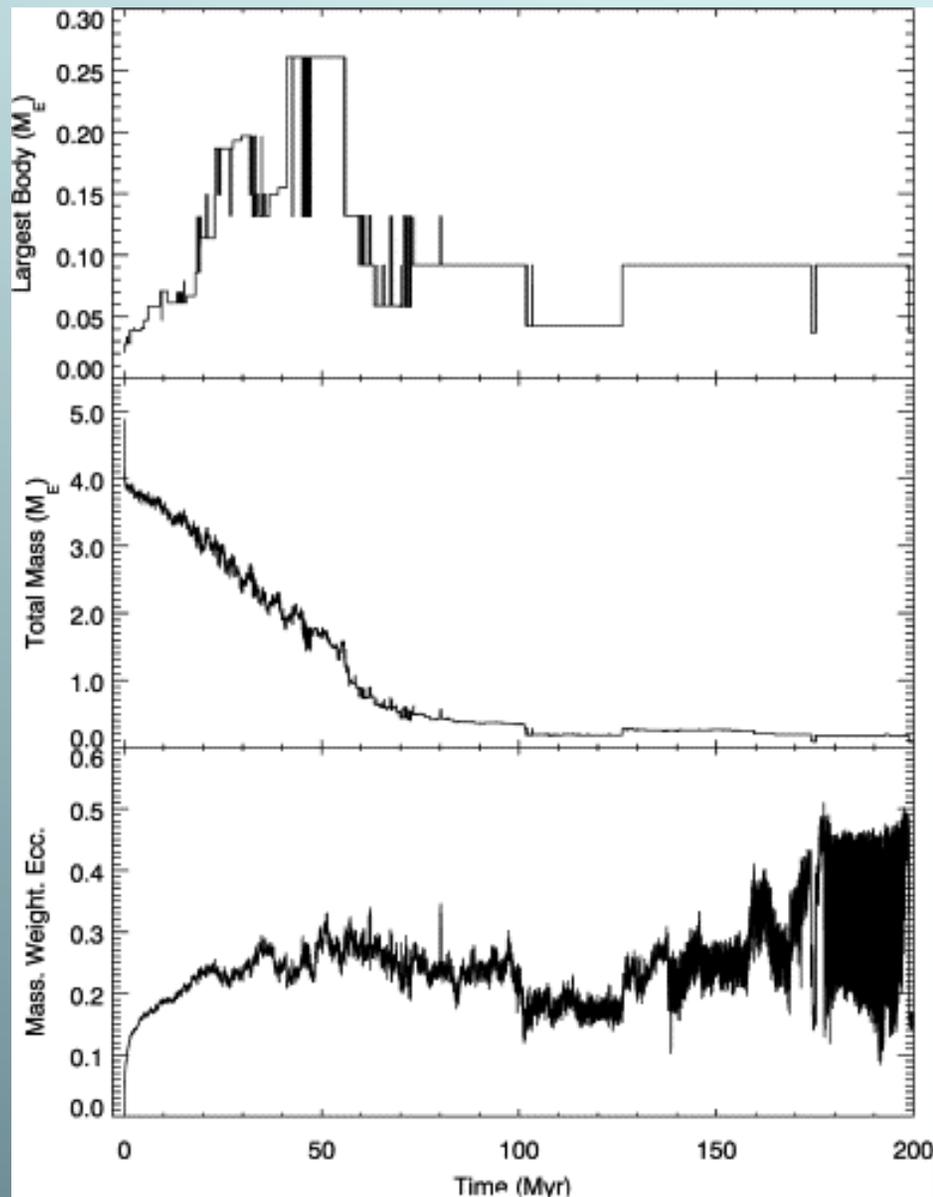


The mean eccentricities for planets *a*, *b*, and *c* from 100–200 Myr are 0.048, 0.039, and 0.057





# Evolution of Asteroid Belt



- Evolution of the asteroid belt (defined as  $2.2 < a < 5.2$  AU) in time for simulation 0. Top: The most massive body in the asteroid belt through time. Middle: Total mass in the asteroid belt as a function of time. Bottom: Mass-weighted eccentricity of all bodies in the asteroid belt over time.

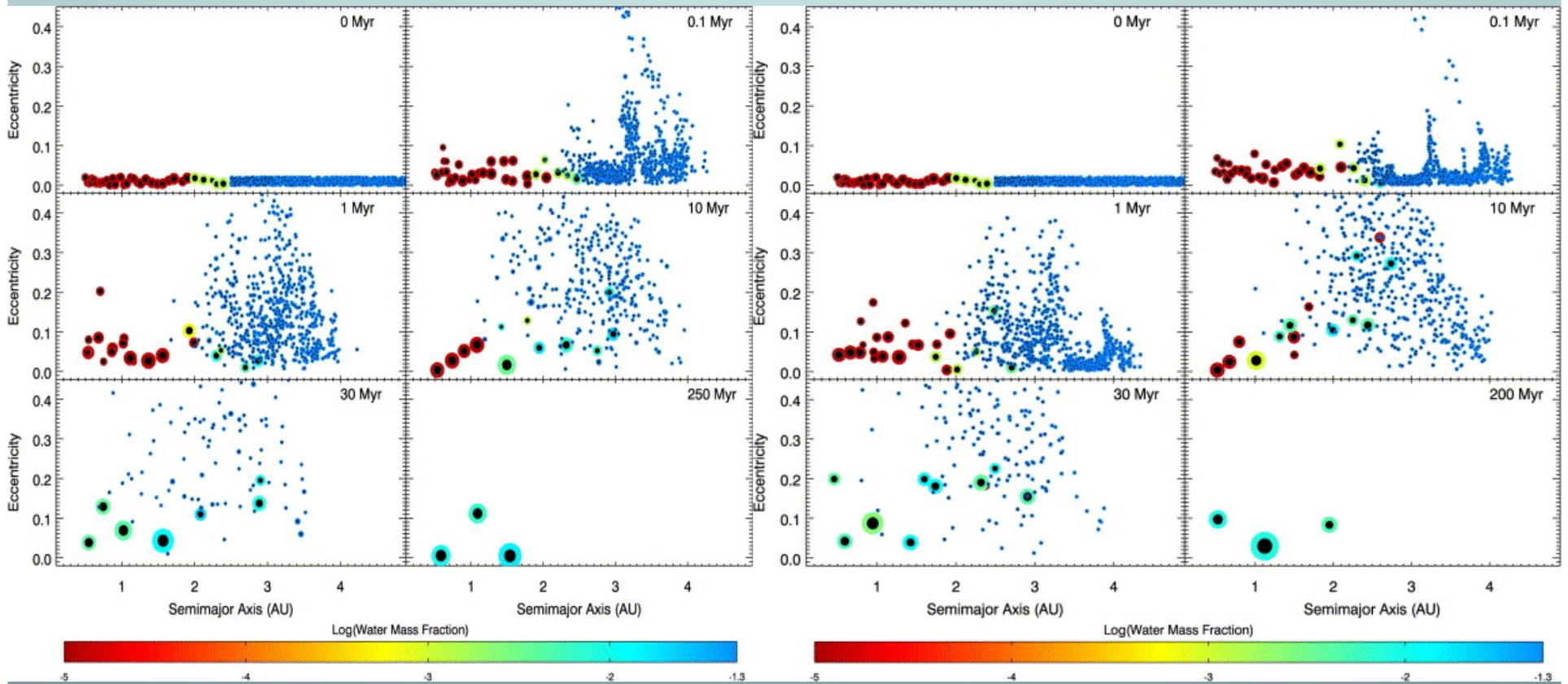
# Simulations 1a and 1b

- 38 – planetary embryos out to 2.5 AU
- 1000 –  $0.006 M_{\text{Earth}}$  “planetesimals” between 2.5 and 5 AU
- Same starting positions
- 1a-planetesimals are massive bodies which interact gravitationally with all other bodies in the simulation
- 1b-planetesimals feel the gravitational presence of the embryos and Jupiter, but not each other's presence. These non-interacting planetesimals may not collide with each other.

# 1a and 1b

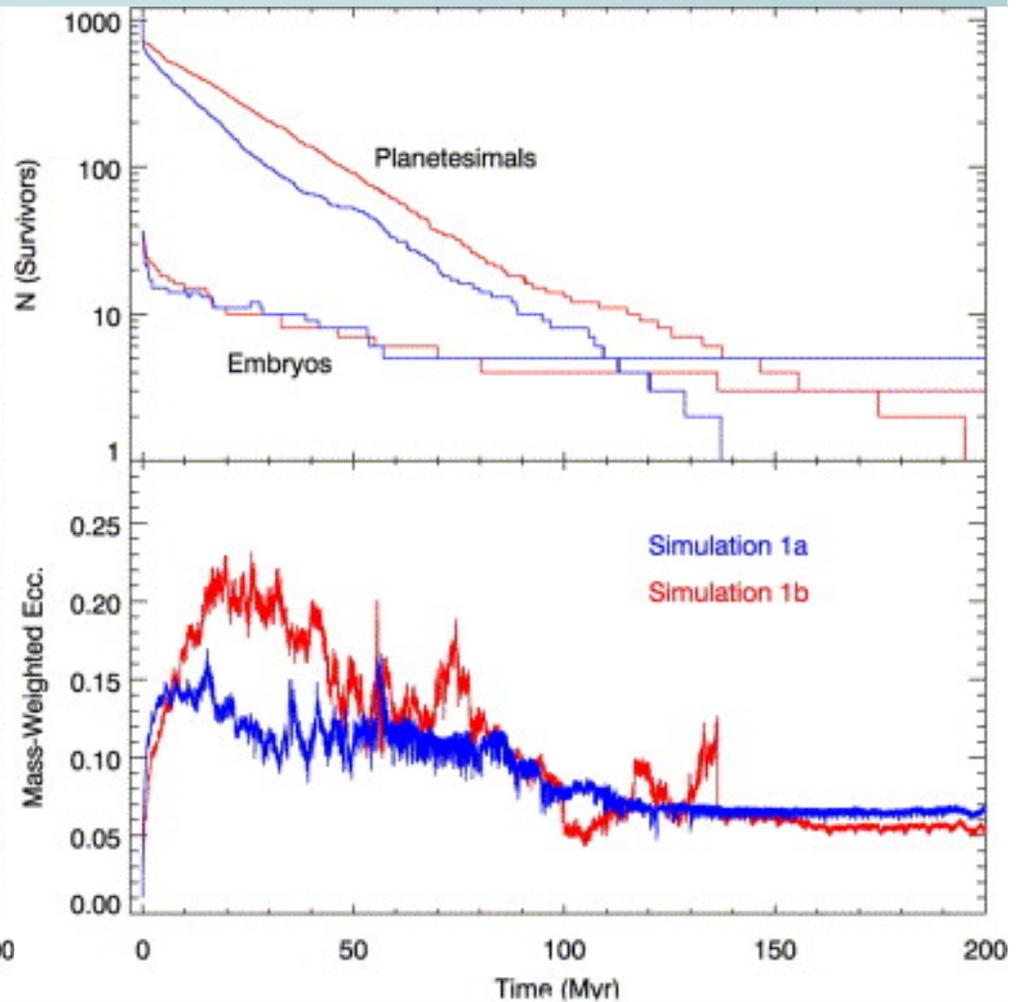
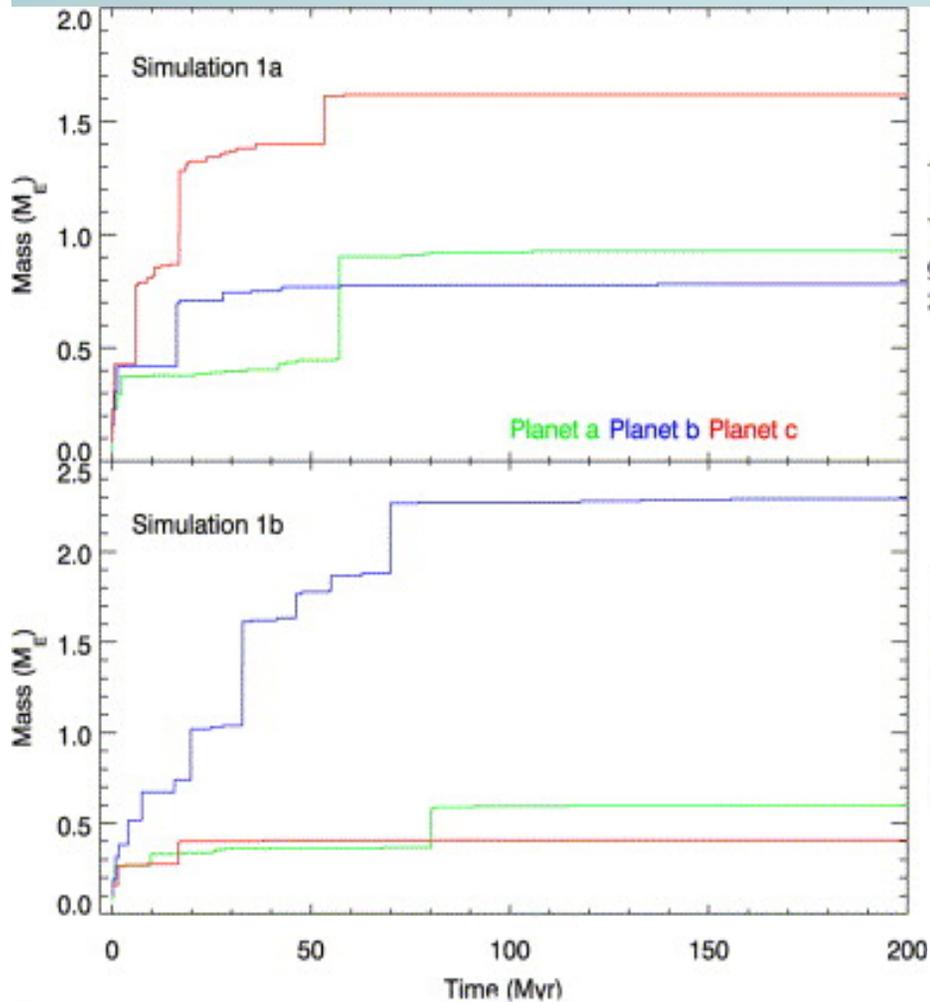
Self Interacting

Non self-interacting



Growth of surviving  
terrestrial planets

Top: Number of surviving  
bodies  
Bottom: mass-weighted  
eccentricity of surviving  
bodies



# 1a and 1b Summary

- Accretion can happen in asteroid belt
- No large embryos formed in asteroid belt
- Run into resolution limit because no planetesimals remain at end of simulations
- Self-gravity accelerates planet formation

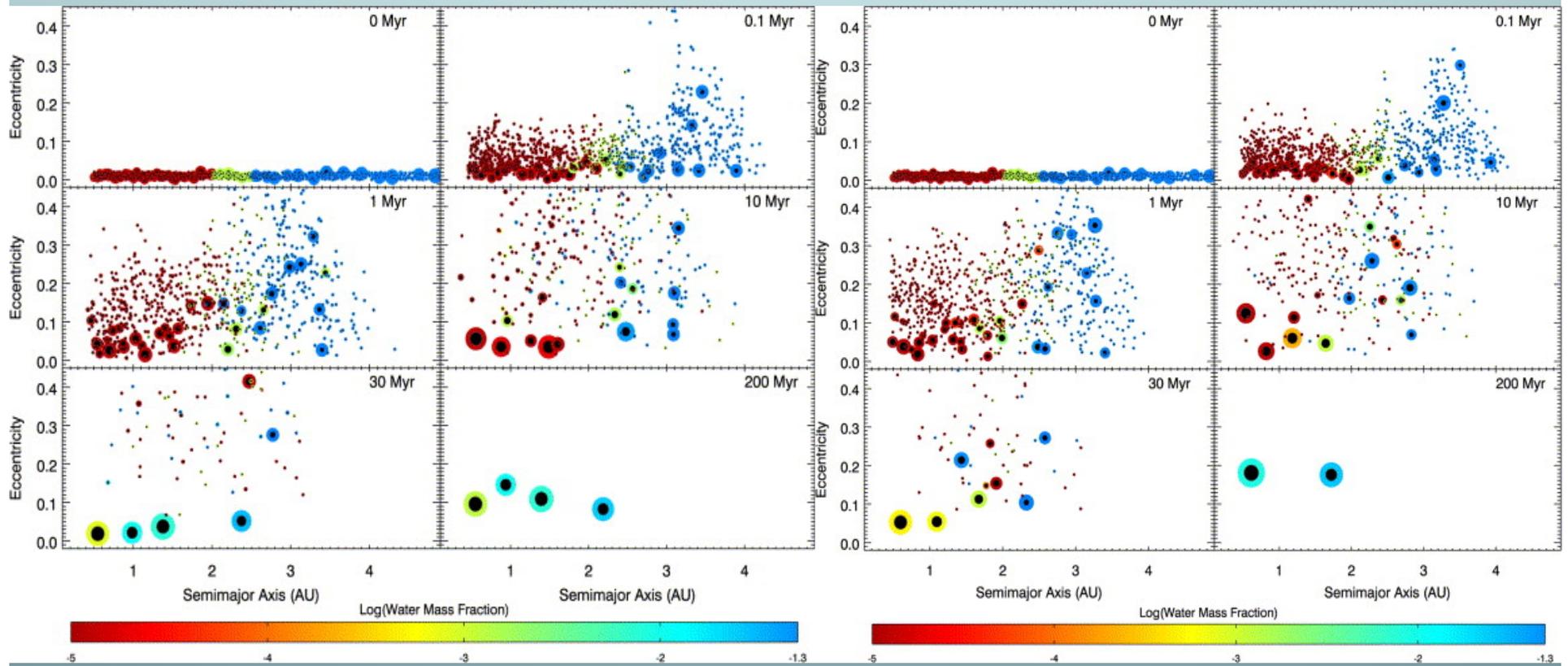
# 2a and 2b Simulations

- 2a and 2b have identical starting conditions
- 54 planetary embryos throughout the terrestrial region, embedded in a disk of 1000 “planetesimals” of  $0.003 M_{\text{earth}}$
- Mass:  $2/3$  – embryos,  $1/3$  – planetesimals.
- Embryos formed all the way out to 5 AU
- 2a all particles are fully self-interacting
- 2b the planetesimals do not feel each other's presence

# 2a and 2b

Self-interacting

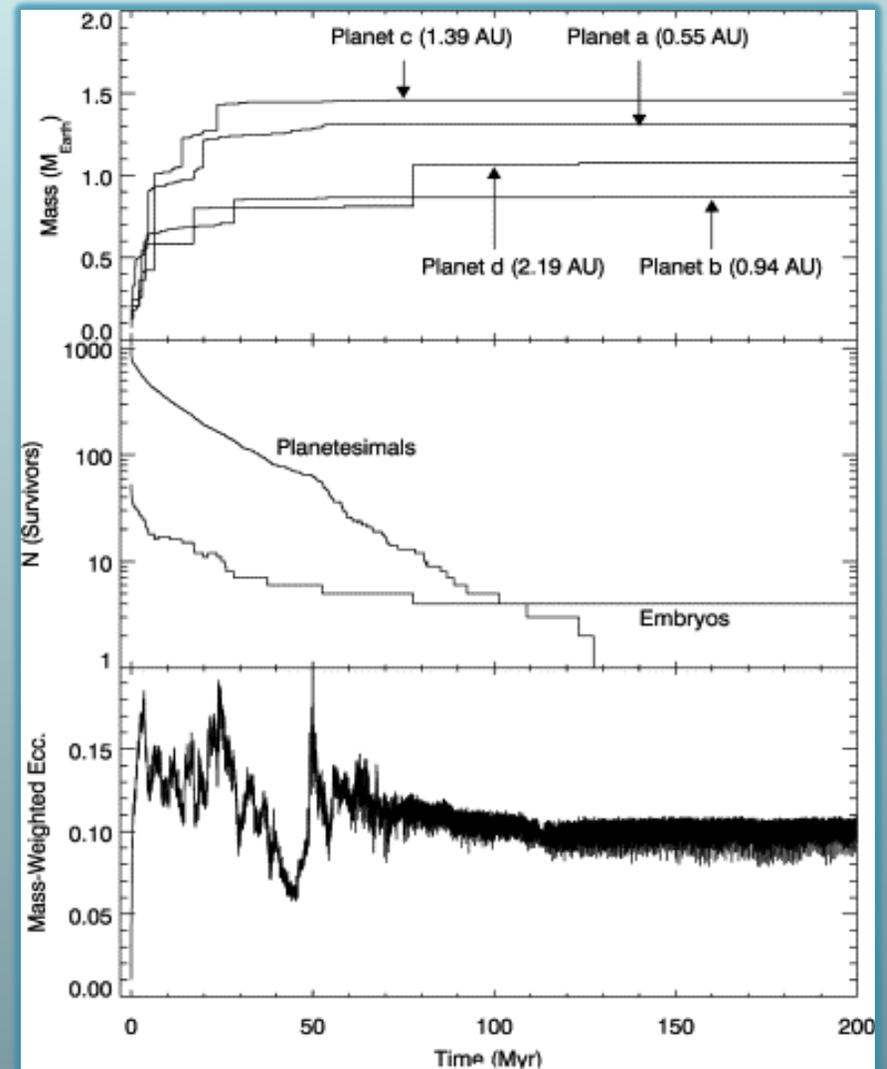
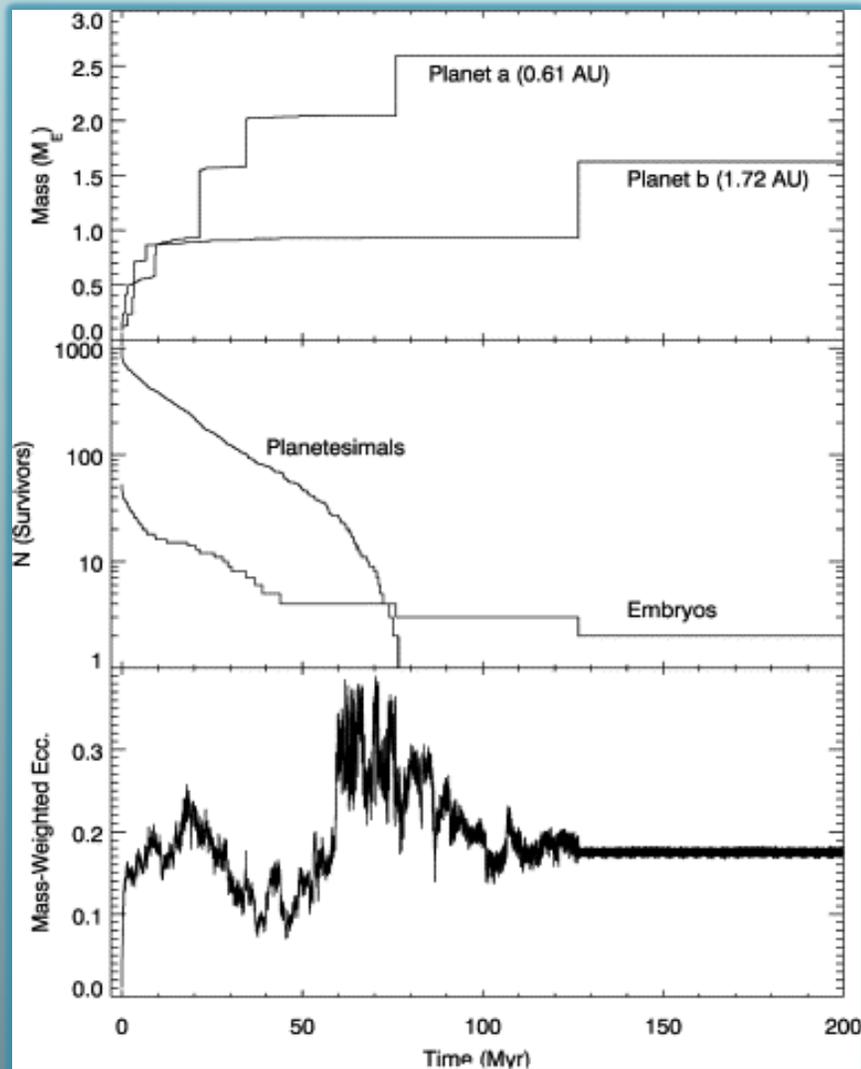
Non-self-interacting



Top: Mass vs Time for surviving planets  
Middle: Number of surviving planetary embryos  
Bottom: Mass-weighted eccentricity of surviving bodies

2b

2a



# Conclusions

- feeding zones of the terrestrial planets widen and move outward in time
- The asteroid belt is cleared of  $>99\%$  of its mass as a natural result of terrestrial accretion.
- Jupiter possibly stunting growth of embryos beyond 2-3AU
- Dynamical friction is important for the growth of terrestrial planets
- smaller eccentricities

Properties of (potentially habitable) planets formed<sup>a</sup>

Simulation	Planet	$a$ (AU)	$\bar{e}^b$	$\bar{i}$ ( $^\circ$ ) <sup>c</sup>	$M$ ( $M_\oplus$ )	W.M.F.	$N$ (oceans) <sup>d</sup>	Fe M.F.
0	a	0.55	0.05	2.8	1.54	$2.6 \times 10^{-3}$	15	0.32
	<b>b</b>	<b>0.98</b>	<b>0.04</b>	<b>2.4</b>	<b>2.04</b>	<b><math>8.4 \times 10^{-3}</math></b>	<b>66</b>	<b>0.28</b>
	c	1.93	0.06	4.6	0.95	$9.1 \times 10^{-3}$	33	0.28
1a	a	0.58	0.05	2.7	0.93	$8.3 \times 10^{-3}$	30	0.31
	<b>b</b>	<b>1.09</b>	<b>0.07</b>	<b>4.1</b>	<b>0.78</b>	<b><math>5.5 \times 10^{-3}</math></b>	<b>17</b>	<b>0.30</b>
	c	1.54	0.04	2.6	1.62	$1.2 \times 10^{-2}$	75	0.26
1b	a	0.52	0.06	8.9	0.60	$7.2 \times 10^{-3}$	17	0.31
	<b>b</b>	<b>1.12</b>	<b>0.05</b>	<b>3.5</b>	<b>2.29</b>	<b><math>6.7 \times 10^{-3}</math></b>	<b>60</b>	<b>0.29</b>
	c	1.95	0.09	9.7	0.41	$3.8 \times 10^{-3}$	6	0.28
2a	a	0.55	0.08	2.6	1.31	$9.3 \times 10^{-4}$	5	0.33
	<b>b</b>	<b>0.94</b>	<b>0.13</b>	<b>3.4</b>	<b>0.87</b>	<b><math>8.6 \times 10^{-3}</math></b>	<b>29</b>	0.29
	<b>c</b>	<b>1.39</b>	<b>0.11</b>	<b>2.4</b>	<b>1.46</b>	<b><math>6 \times 10^{-3}</math></b>	<b>34</b>	0.29
	d	2.19	0.08	8.8	1.08	$1.8 \times 10^{-2}$	75	0.24
2b	a	0.61	0.18	13.1	2.60	$7.1 \times 10^{-3}$	71	0.30
	b	1.72	0.17	0.5	1.63	$2.0 \times 10^{-2}$	126	0.22
Mercury <sup>e</sup>		0.39	0.19	7.0	0.06	$1 \times 10^{-5}$	0	0.68
Venus		0.72	0.03	3.4	0.82	$5 \times 10^{-4}$	1.5	0.33
<b>Earth</b>		<b>1.0</b>	<b>0.03</b>	<b>0.0</b>	<b>1.0</b>	<b><math>1 \times 10^{-3}</math></b>	<b>4</b>	<b>0.34</b>
Mars		1.52	0.08	1.9	0.11	$2 \times 10^{-4}$	0.1	0.29